

What you'll Learn About

- Average Rates of Change
- A Definition of the Derivative

$$\frac{ft}{sec} = \frac{\Delta \text{ in distance}}{\Delta \text{ in time}}$$

An object dropped from rest from the top of a tall building falls $y = 16t^2$ feet in the first t seconds. Find the **average speed/average rate of change** during the first 2 seconds of flight.

$$t=0 \quad t=2$$

$$d=0 \quad d=16(2)^2=64$$

$$\frac{64-0}{2-0} = \frac{64}{2} = 32 \frac{ft}{sec}$$

difference quotient

Find the average rate of change of $f(x) = \sqrt{4x+1}$ over each interval

a) $[0, 2]$

$$x=0 \quad y=1$$

$$x=2 \quad y=3$$

$$A.R.O.C = \frac{3-1}{2-0}$$

$$= \frac{2}{2}$$

$$= 1$$

b) $[10, 12]$

$$x=10 \quad y=\sqrt{41}$$

$$x=12 \quad y=7$$

$$A.R.O.C = \frac{7-\sqrt{41}}{12-10}$$

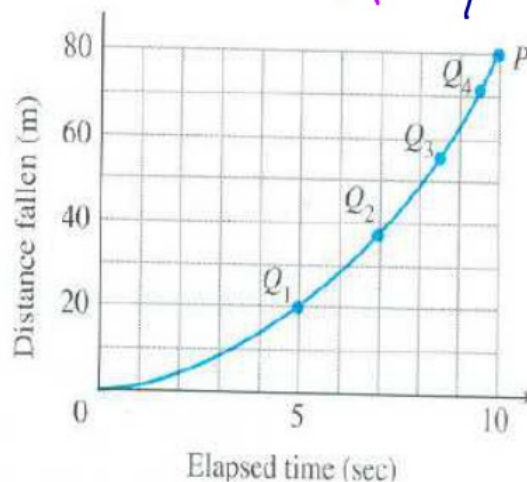
Estimate the average rate of change by finding the slopes of each secant line. Indicate units of measure

PQ1=

PQ2=

PQ3=

PQ4=



- Q1(5,20)
- Q2(7,38)
- Q3(8.5, 55)
- Q4(9.5,71)
- P(10,80)

Use the slopes of the secant lines to Estimate the instantaneous rate of change/slope at point P

What you'll Learn About

- How the derivative might fail to exist
- Differentiability implies local linearity
- Differentiability implies Continuity

Continuous
 Slope is defined

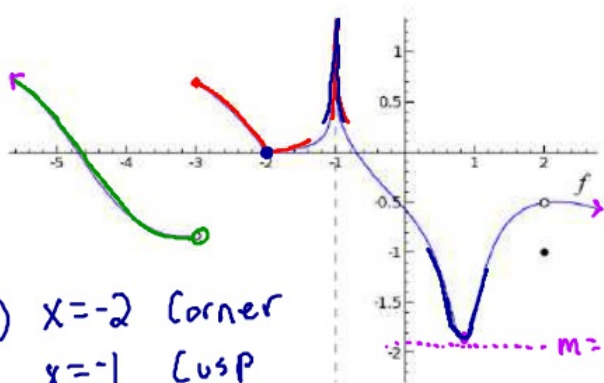
Not Differentiable

- $x = -3$ Jump
- $x = -1$ Cusp
- $x = -2$ Corner
- $x = 2$ Hole

Not Continuous

- $x = -3$ Jump
- $x = 2$ Hole

- Find all points where the function, $f(x)$, is differentiable.
- Find all points where the function is continuous, but not differentiable.
- Find all points where the graph is neither continuous nor differentiable.



Vertical Tangent
 Cusps
 Corner

jumps
 Hole
 VA

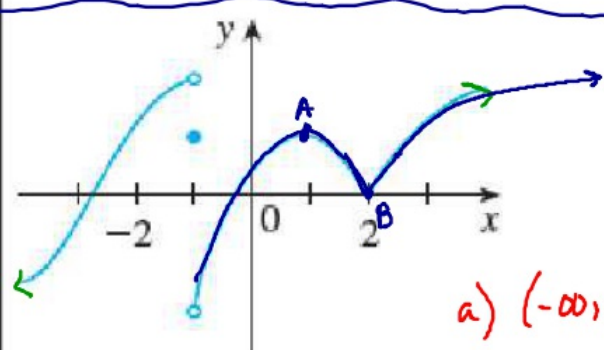
- $x = -2$ Corner
 $x = -1$ Cusp

- $x = -3, x = +2$

- $(-\infty, -3) \cup (-3, -2) \cup (-2, -1) \cup (-1, 2) \cup (2, \infty)$

Not Differentiable

- $x = -1$ Jump
- $x = 2$ Cusp or Corner



- $(-\infty, -1) \cup (-1, 2) \cup (2, \infty)$

- $x = 2$

Not Continuous

- $x = -1$ Jump

- $x = -1$

Not Differentiable

$x = -2$ Corner/Cusp

$x = 1$ Jump

$x = 4$ VA

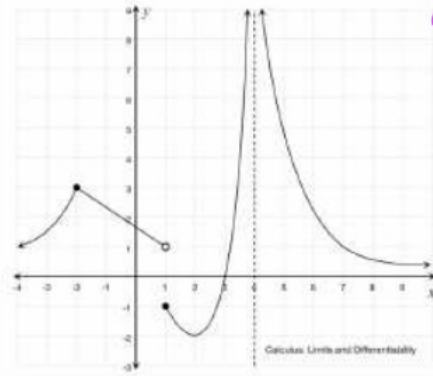
Not Continuous

$x = 1$ Jump

$x = 4$ VA

3.2 Differentiability:

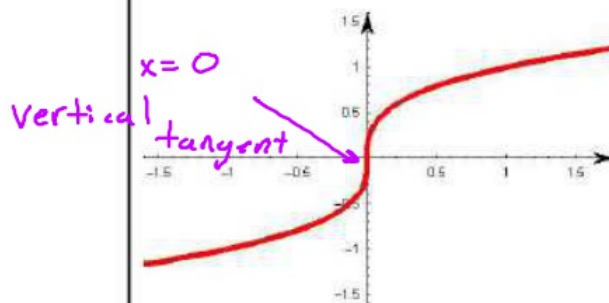
- Find all points where the function, $f(x)$, is differentiable.
- Find all points where the function is continuous, but not differentiable.
- Find all points where the graph is neither continuous nor differentiable.



a) $(-\infty, -2) \cup (-2, 1) \cup (1, 4) \cup (4, \infty)$

b) $x = -2$

c) $x = 1$ $x = 4$



continuous $(-\infty, \infty)$

not differentiable
 $x = 0$

